

Characterizing the **chaotic** variability of the global eddying ocean and its atmospheric modulation



sea-level **chaotic** variability (-20/+20cm)
(seasonally-forced NEMO 1/4° simulation)

Thierry Penduff¹,

S. Leroux¹, S. Close¹, I. Garcia-Gomez¹,

S. Grégorio¹, I. Benabicha¹,

B. Barnier¹, J.M. Molines¹

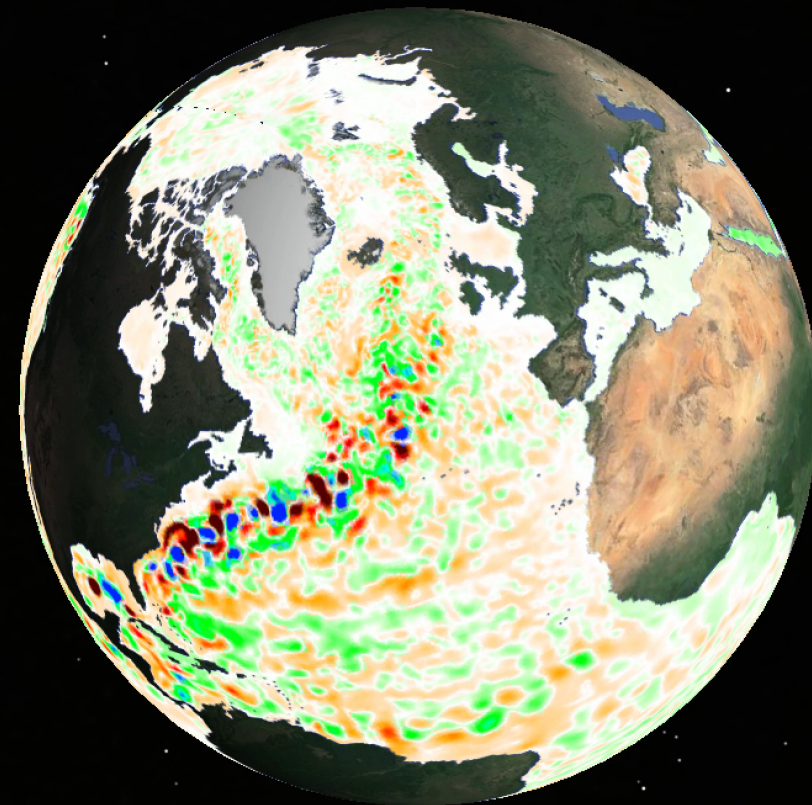
G. Sérazin^{1, 2},

L. Bessières², L. Terray²

¹IGE,
Grenoble



²CERFACS,
Toulouse



Low-Freq. **Chaotic** Intrinsic Variability (**LFCIV**): idealized

Constant/seasonal wind forcing : Increased $Re \rightarrow$

Spontaneous emergence of **LFCIV** (1-10 year)

Dijkstra & Ghil 2005; Sushama et al 2007

- **Western boundary current systems**

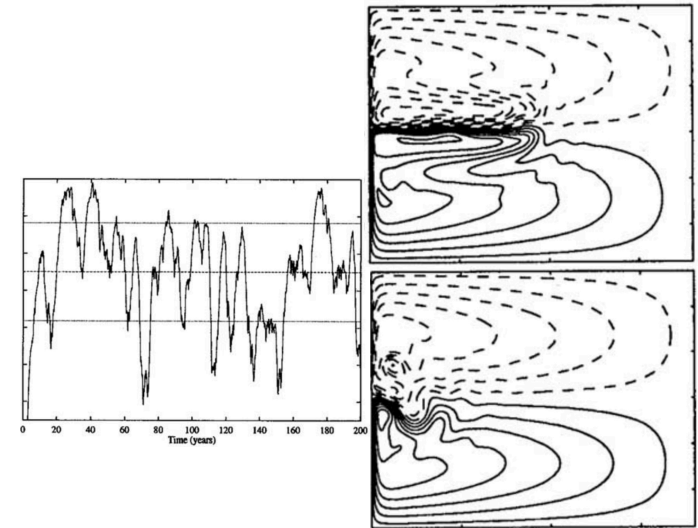
- Surface jets, DWBC, Recirculation gyres (shape, strength)

Dewar 2003; Spall 1996; etc

- Mode waters (low-PV pool volume)

- Rossby modes

Hazeleger & Drijfhout 2000



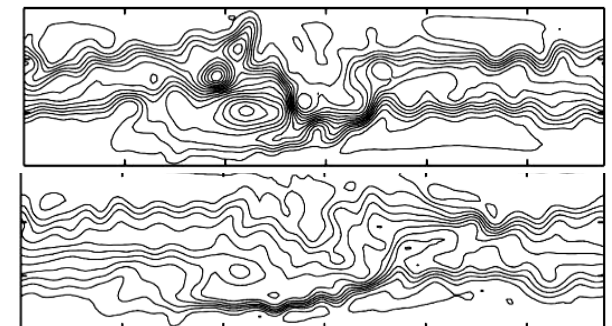
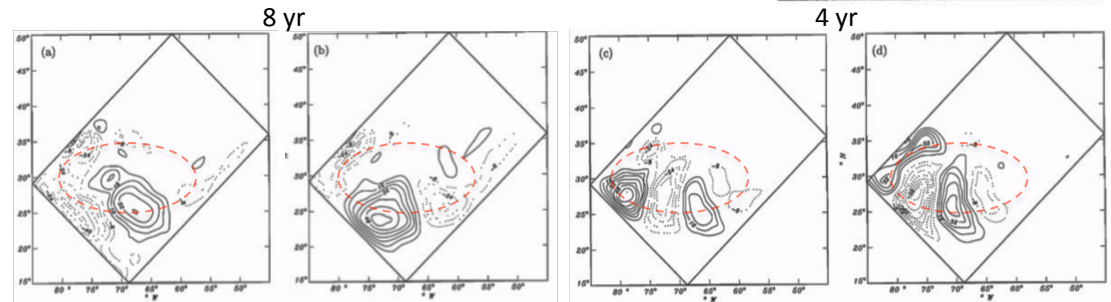
- **ACC**

Current / eddy / topography interactions

- path, transport

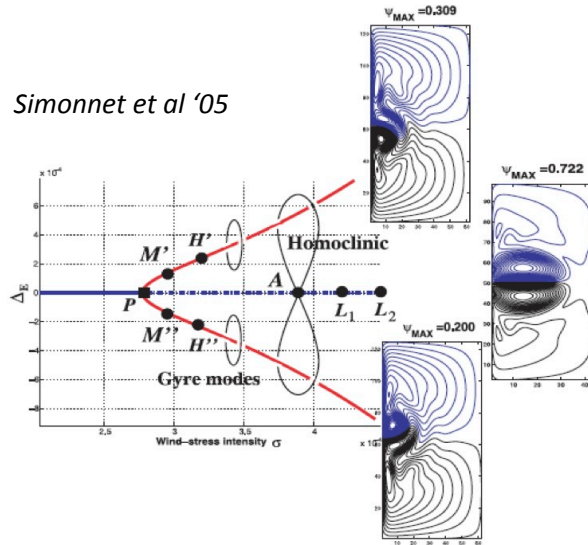
- jet jumping & migration

Hogg & Blundell 2006; Thompson & Richards 2011; etc



LFCIV: 2 main nonlinear paradigms

Simonnet et al '05



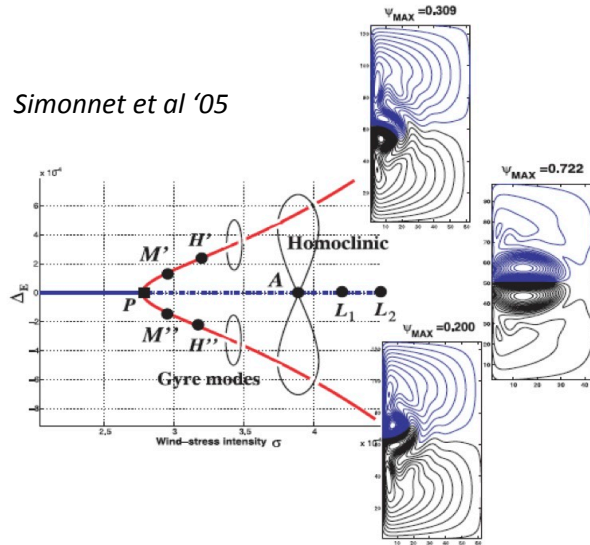
1. Spontaneous transitions between large-scale equilibria

(DST, bifurcation studies, etc : e.g. Dijkstra and Ghil 2005, and ref. therein)

- ✓ Mean APE field $\xrightarrow{\text{Somehow}}$ Low-freq intrinsic variability
- ✓ Re number increases \longrightarrow Chaotic transitions
- ✓ Mesoscale eddies provide ambient «noise» but are not crucial

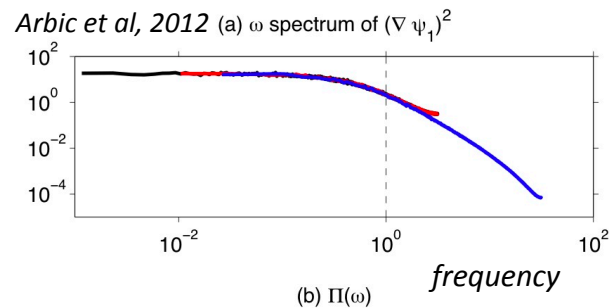
$\longrightarrow Re$

LFCIV: 2 main nonlinear paradigms



→ Re

laminar → mesoscale eddies



1. Spontaneous transitions between large-scale equilibria

(DST, bifurcation studies, etc : e.g. Dijkstra and Ghil 2005, and ref. therein)

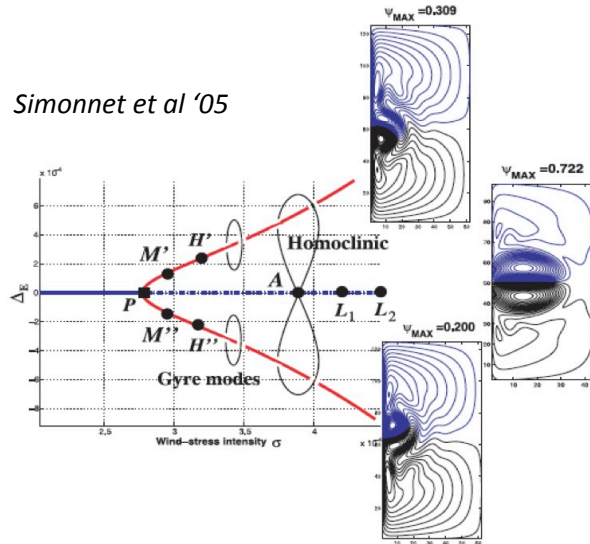
- ✓ Mean APE field $\xrightarrow{\text{Somehow}}$ Low-freq intrinsic variability
- ✓ Re number increases \longrightarrow Chaotic transitions
- ✓ Mesoscale eddies provide ambient «noise» but **are not crucial**

2. Direct eddy forcing

(PV fluxes, inverse cascades : e.g. Berloff et al 2007, Arbic et al 2012, Spall 1996)

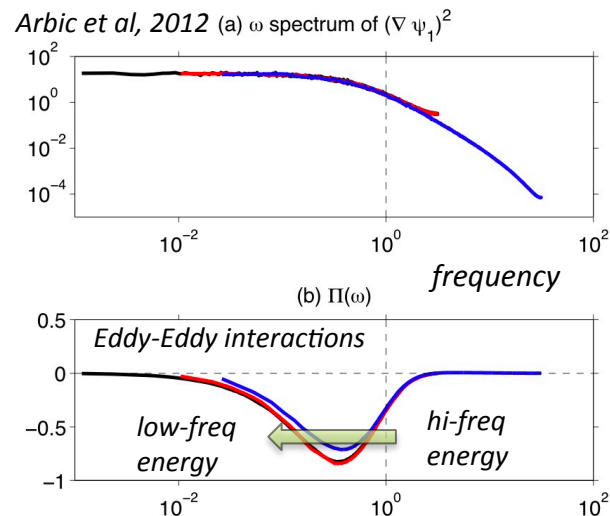
- ✓ Mean APE field $\xrightarrow{\text{Eddies}}$ Low-freq intrinsic variability
- ✓ Re number increases \longrightarrow Stronger eddy fluxes
- ✓ Mesoscale eddies rectify the flow and **drive LFCIV**

LFCIV: 2 main nonlinear paradigms



→ Re

laminar → mesoscale eddies



1. Spontaneous transitions between large-scale equilibria

(DST, bifurcation studies, etc : e.g. Dijkstra and Ghil 2005, and ref. therein)

- ✓ Mean APE field $\xrightarrow{\text{Somehow}}$ Low-freq intrinsic variability
- ✓ Re number increases \longrightarrow Chaotic transitions
- ✓ Mesoscale eddies provide ambient «noise» but **are not crucial**

2. Direct eddy forcing

(PV fluxes, inverse cascades : e.g. Berloff et al 2007, Arbic et al 2012, Spall 1996)

- ✓ Mean APE field $\xrightarrow{\text{Eddies}}$ Low-freq intrinsic variability
- ✓ Re number increases \longrightarrow Stronger eddy fluxes
- ✓ Mesoscale eddies rectify the flow and **drive LFCIV**

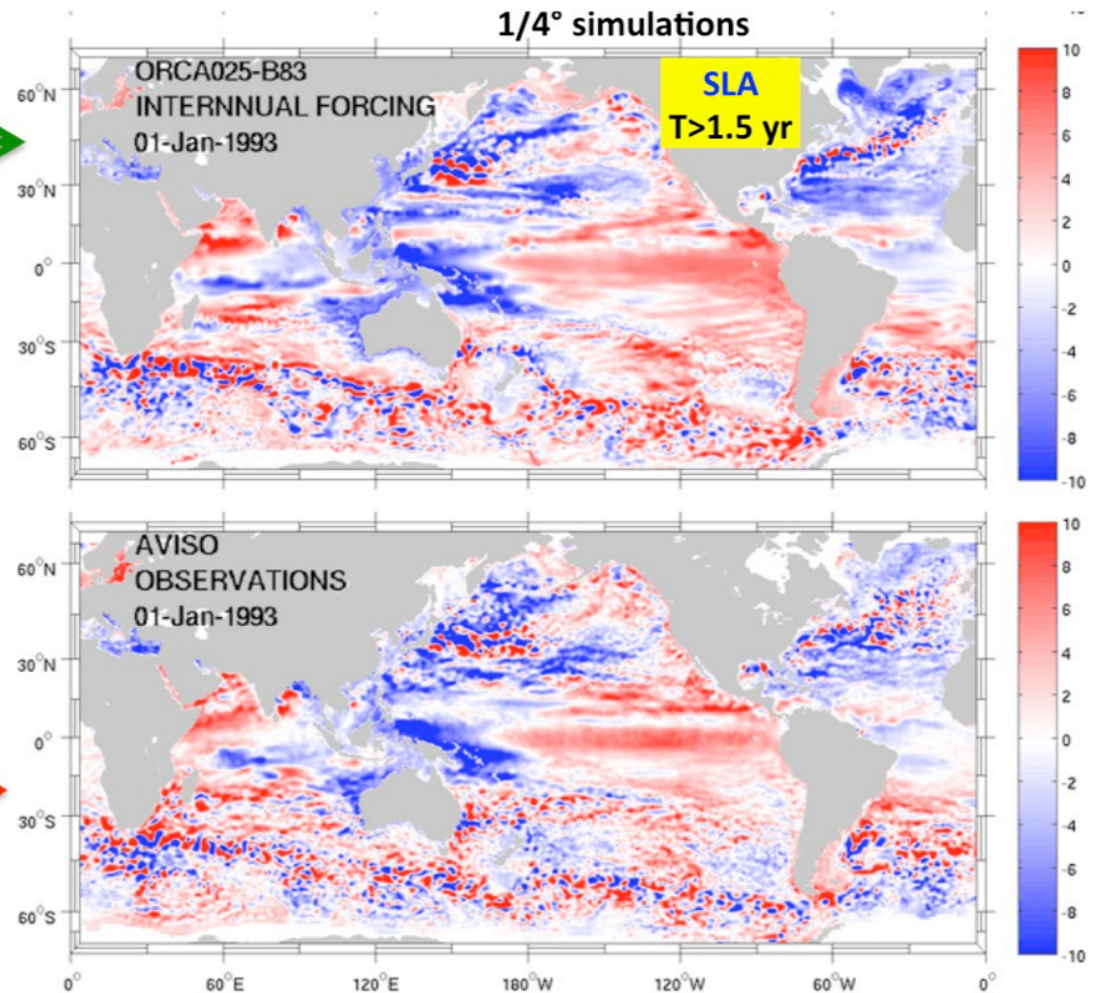
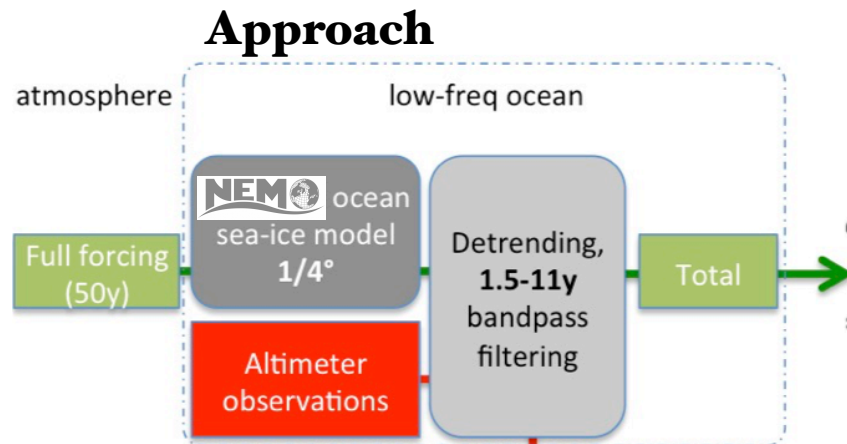
LFCIV in a global, realistic, eddying OGCM ?
(imprints, strength, origin, implications)

Outline

Low-Freq Chaotic Intrinsic Variability in the global ocean

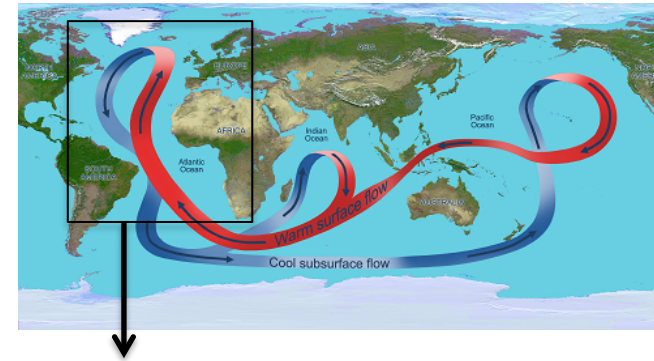
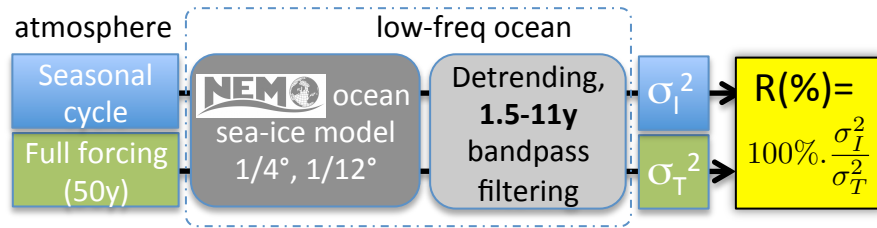
1. **LFCIV** isolated under seasonal forcing
 - Imprint on observed fields (Sea-level, AMOC)
 - A possible generation mechanism
2. **LFCIV** modulated by full (reanalyzed) forcing
 - OCCIPUT Ensemble simulations
 - Sea-level, OHC, AMOC
3. New directions and challenges
 - Non-gaussianity, information theory
 - Ocean chaos \leftrightarrow atmosphere
 - Multivariate analyses (MHT – OHC – Qnet)
4. Conclusions and perspectives

Low-frequency SLA variab. Experimental strategy



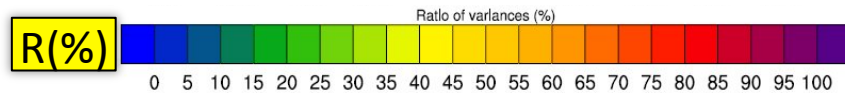
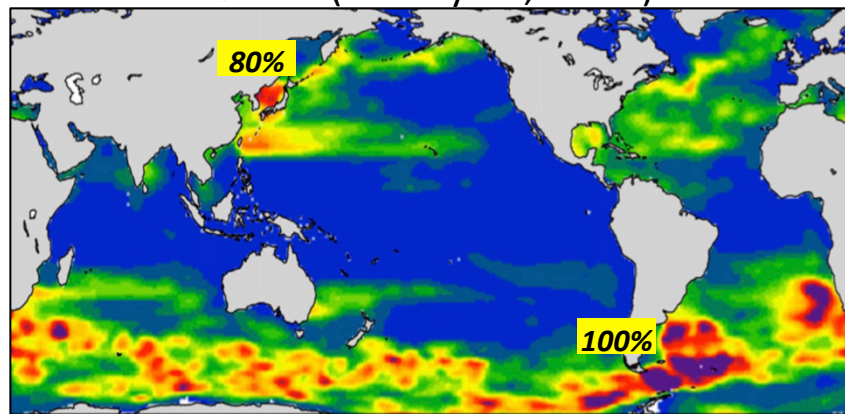
Brodeau et al (Ocean Mod. 2010)
Penduff et al (Jclim 2011)
Sérazin et al (Jclim 2015)

Chaotic part (%) of the large-scale low-frequency variance

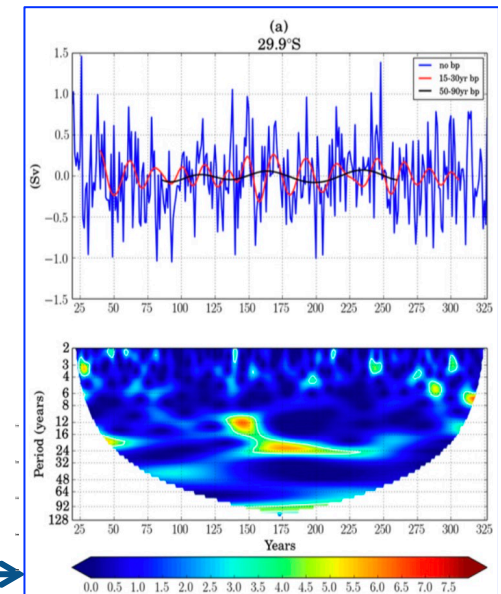
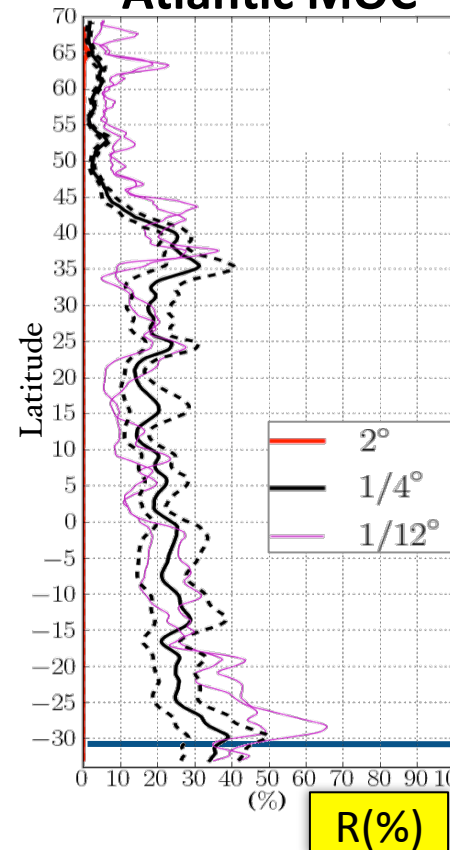


2° simulations : R ~ 0%

SLA (T>1.5 year, L>12°)



Atlantic MOC



Penduff et al (Jclim 2011)

Sérazin et al (Jclim 2015)

Grégorio et al (JPO 2015)

Outline

Low-Freq Chaotic Intrinsic Variability in the global ocean

1. LFCIV isolated under seasonal forcing

- Imprint on observed fields (Sea-level, AMOC)
- A possible generation mechanism

2. LFCIV modulated by full (reanalyzed) forcing

- OCCIPUT Ensemble simulations
- Sea-level, OHC, AMOC

3. New directions and challenges

- Non-gaussianity, information theory
- Ocean chaos \leftrightarrow atmosphere
- Multivariate analyses (MHT – OHC – Qnet)

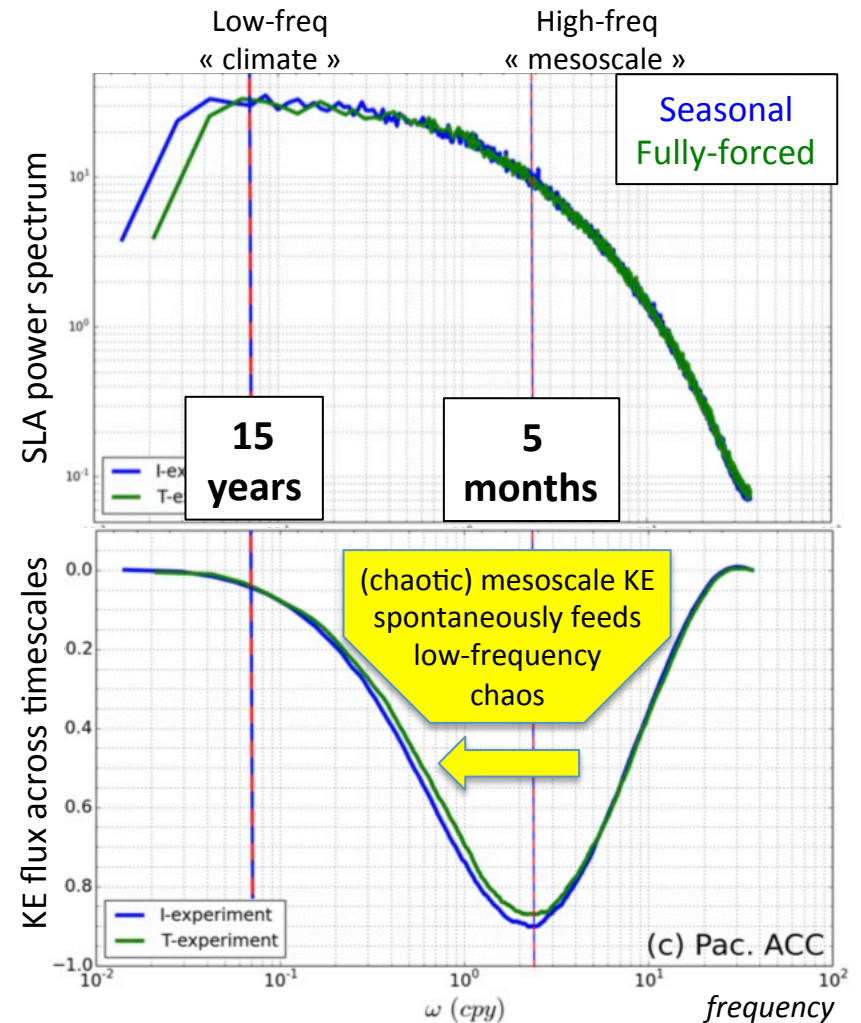
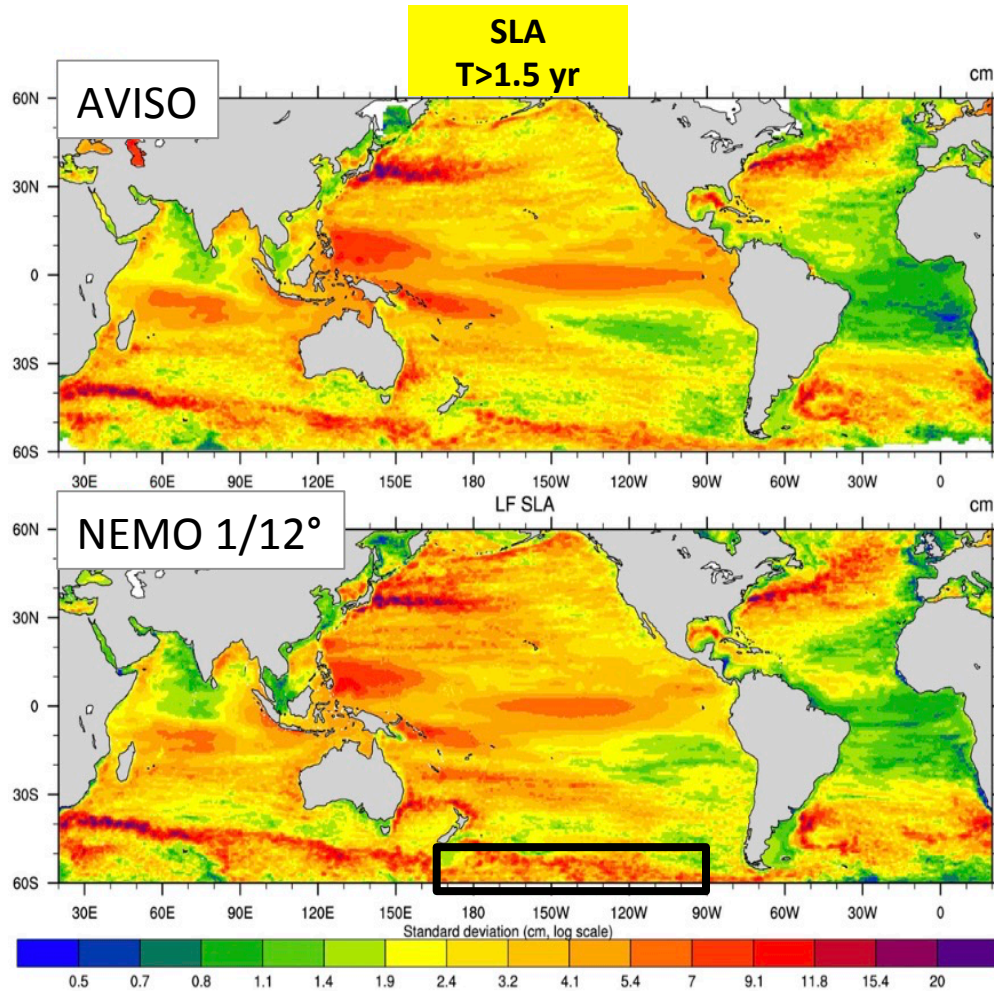
4. Conclusions and perspectives

A source of low-freq **Chaotic** variability : Temporal inverse cascade

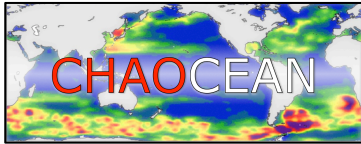
$$T_{KE}(k, l, \omega) = \text{Re}\{J(\widehat{\psi}, \nabla^2 \widehat{\psi}) \cdot \widehat{\psi}^*\},$$

$$\Pi_{KE}(\omega) = \int_{\omega \leq \Omega \leq \omega_N} \left(\int_{-k_N}^{k_N} \int_{-l_N}^{l_N} T_{KE}(k, l, \Omega) dk dl \right) d\Omega$$

Fully-forced 1/12° simulation : low-freq SLA std



Low-freq **Chaotic Intrinsic** variability

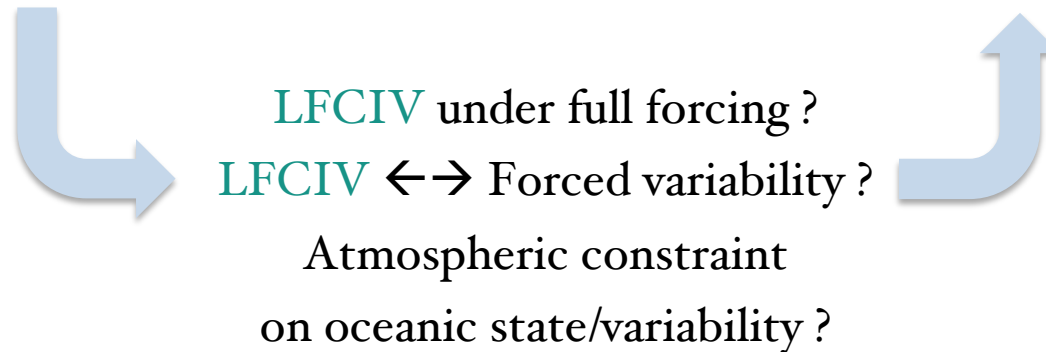


LFCIV isolated under seasonal forcing

- Strong
- Broad range of scales
- Multiple imprints on climate indices

LFCIV under full (reanalyzed) forcing

- Ensemble simulation
- Perturbed initial conditions
- Same forcing on all members



Outline

Low-Freq Chaotic Intrinsic Variability in the global ocean

1. LFCIV isolated under seasonal forcing

- Imprint on observed fields (Sea-level, AMOC)
- A possible generation mechanism

2. LFCIV modulated by full (reanalyzed) forcing

- OCCIPUT Ensemble simulations
- Sea-level, OHC, AMOC

3. New directions and challenges

- Non-gaussianity, information theory
- Ocean chaos \leftrightarrow atmosphere
- Multivariate analyses (MHT – OHC – Qnet)

4. Conclusions and perspectives

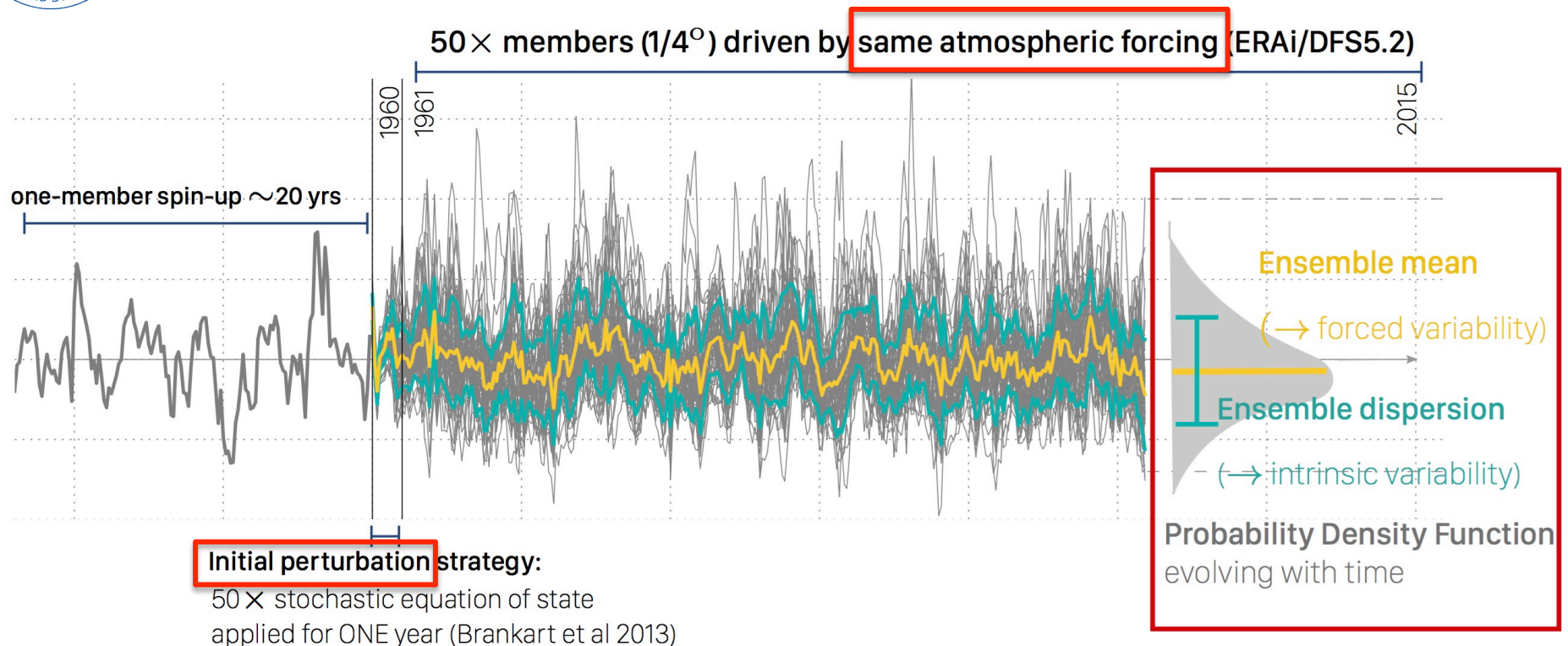
OCCIPUT ensemble simulations

Resources



50-member $\frac{1}{4}^\circ$ ensemble hindcasts :

- Global ocean (56 years)
- North Atlantic (20 years)

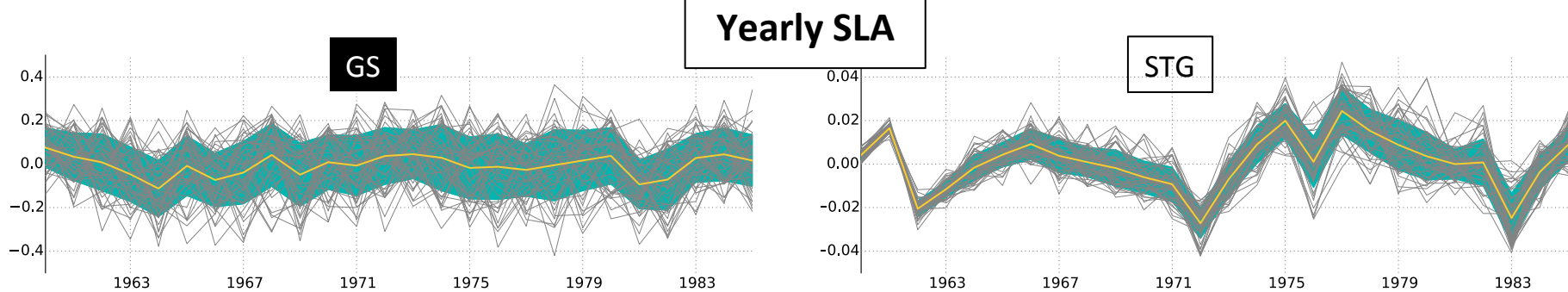
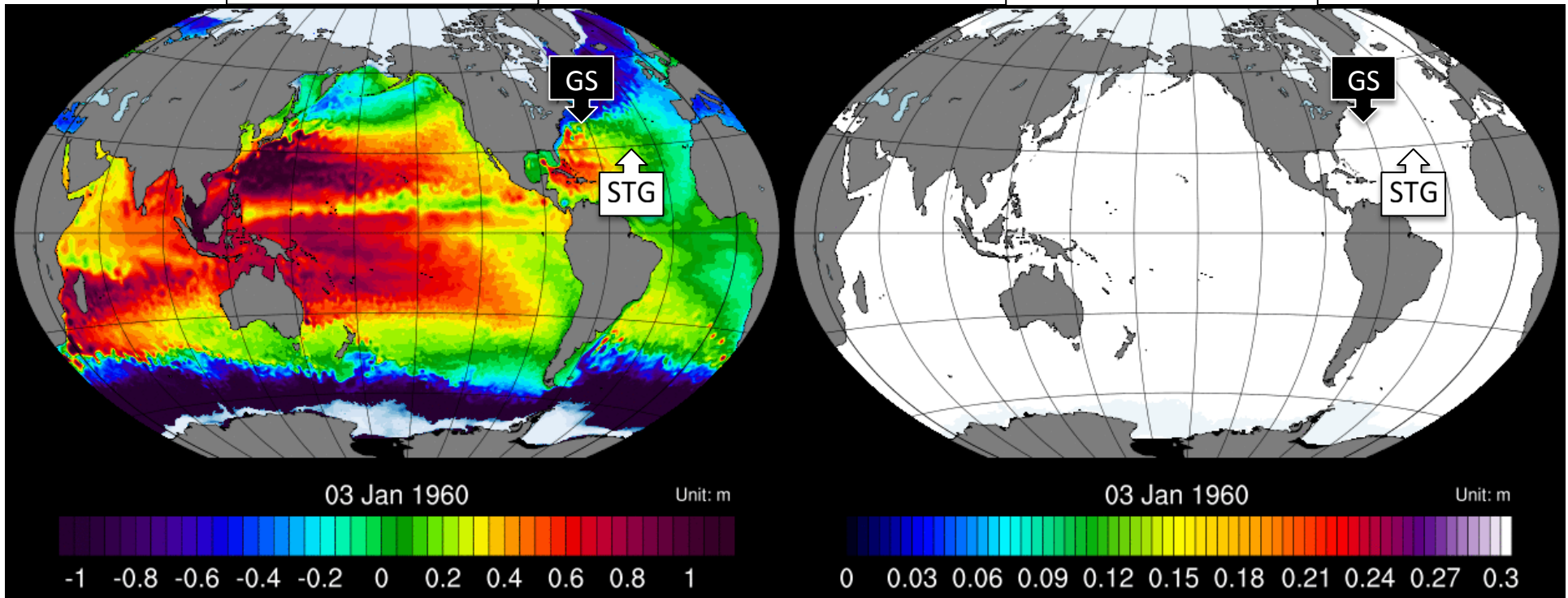


Penduff et al (CLIVAR exch., 2014)
Bessières et al (GMD 2017)

5-day SLA: Forced & Chaotic variability (1960-1965)

Ensemble Mean
FORCED variability

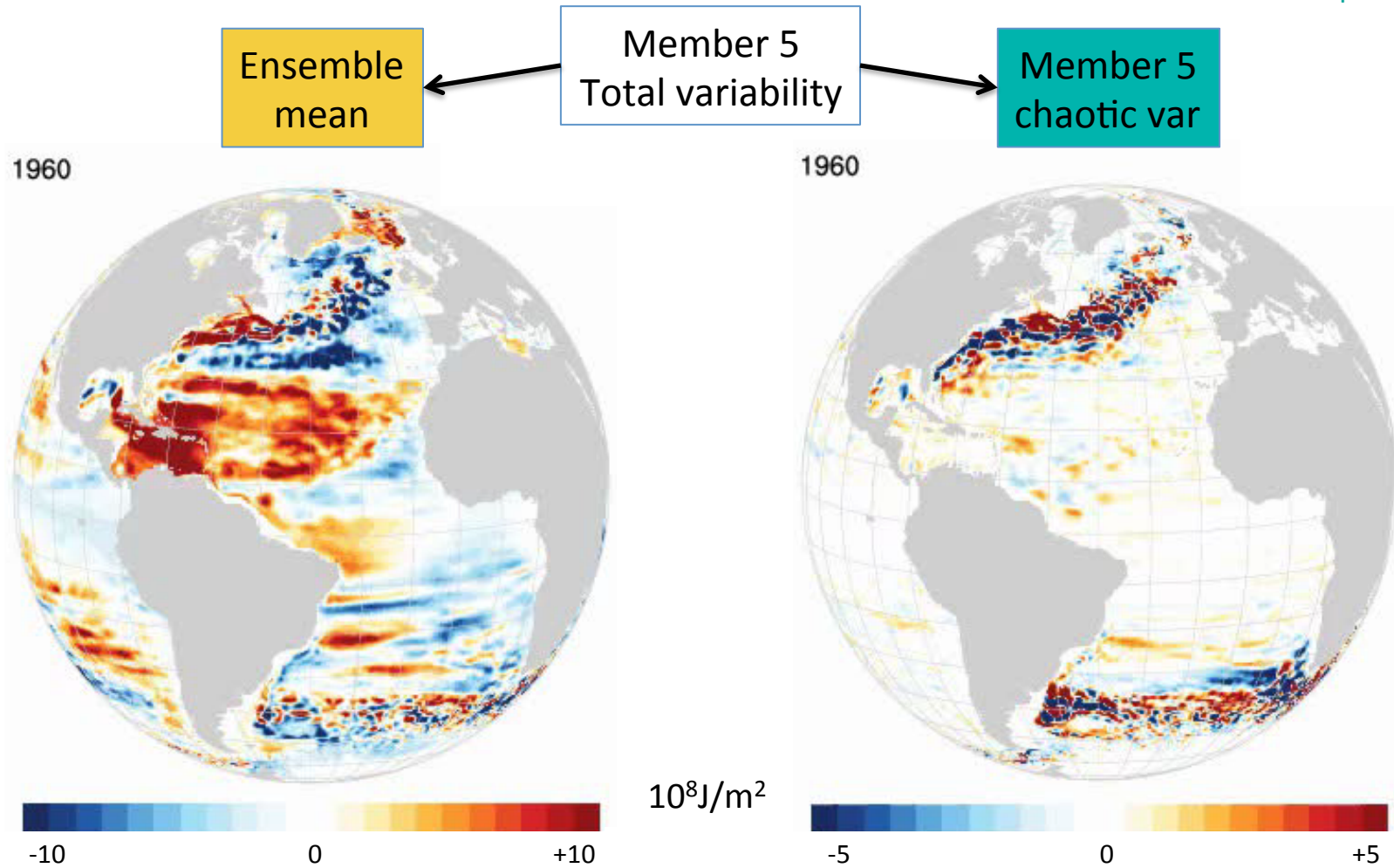
Ensemble STD
CHAOTIC variability



2-15 yr OHC_{0-700m} **Forced & Chaotic** variability (1980-2010)

$$OHC = \rho \cdot C_p \int_{-700}^{surf} T(z) \cdot dz \quad yr = 1980, 2010 \quad member = 1, 50$$

Zero in 2° simulations.
Large potential impact on
atmosphere/climate



2-15 yr OHC_{0-700m} Forced & Chaotic variability (1980-2010)

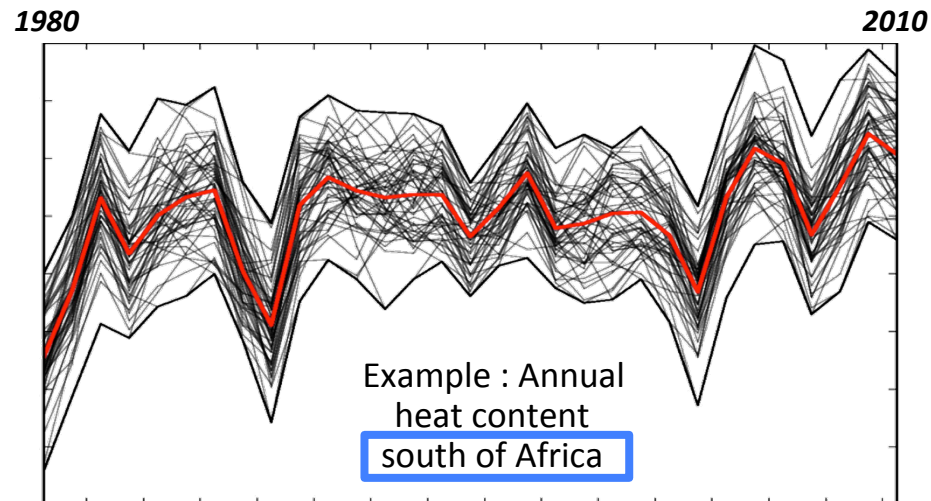
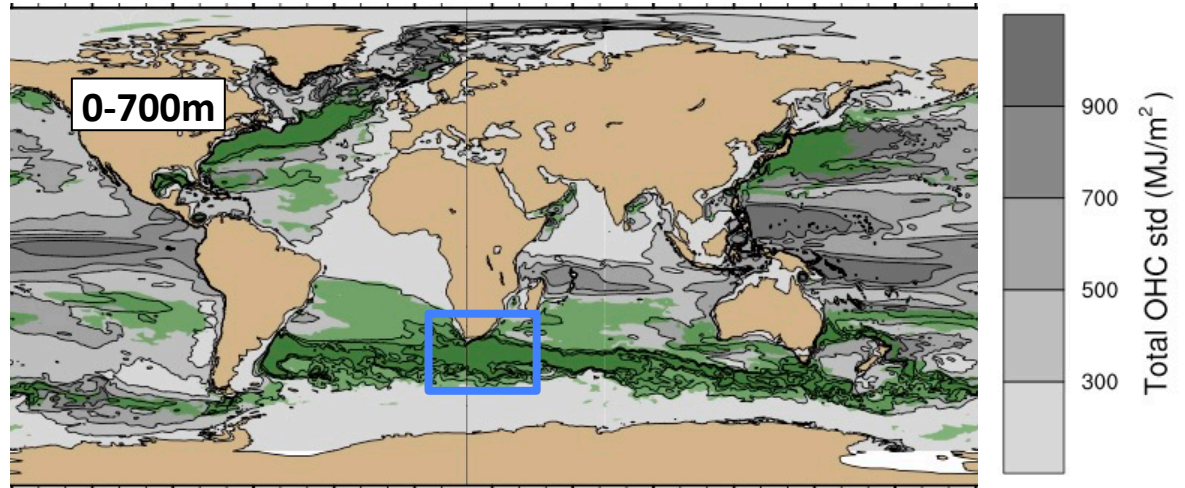
$$OHC = \rho \cdot C_p \int_{-700}^{surf} T(z) \cdot dz \quad yr = 1980, 2010 \quad member = 1, 50$$

Emean (Tstd) → Total var.

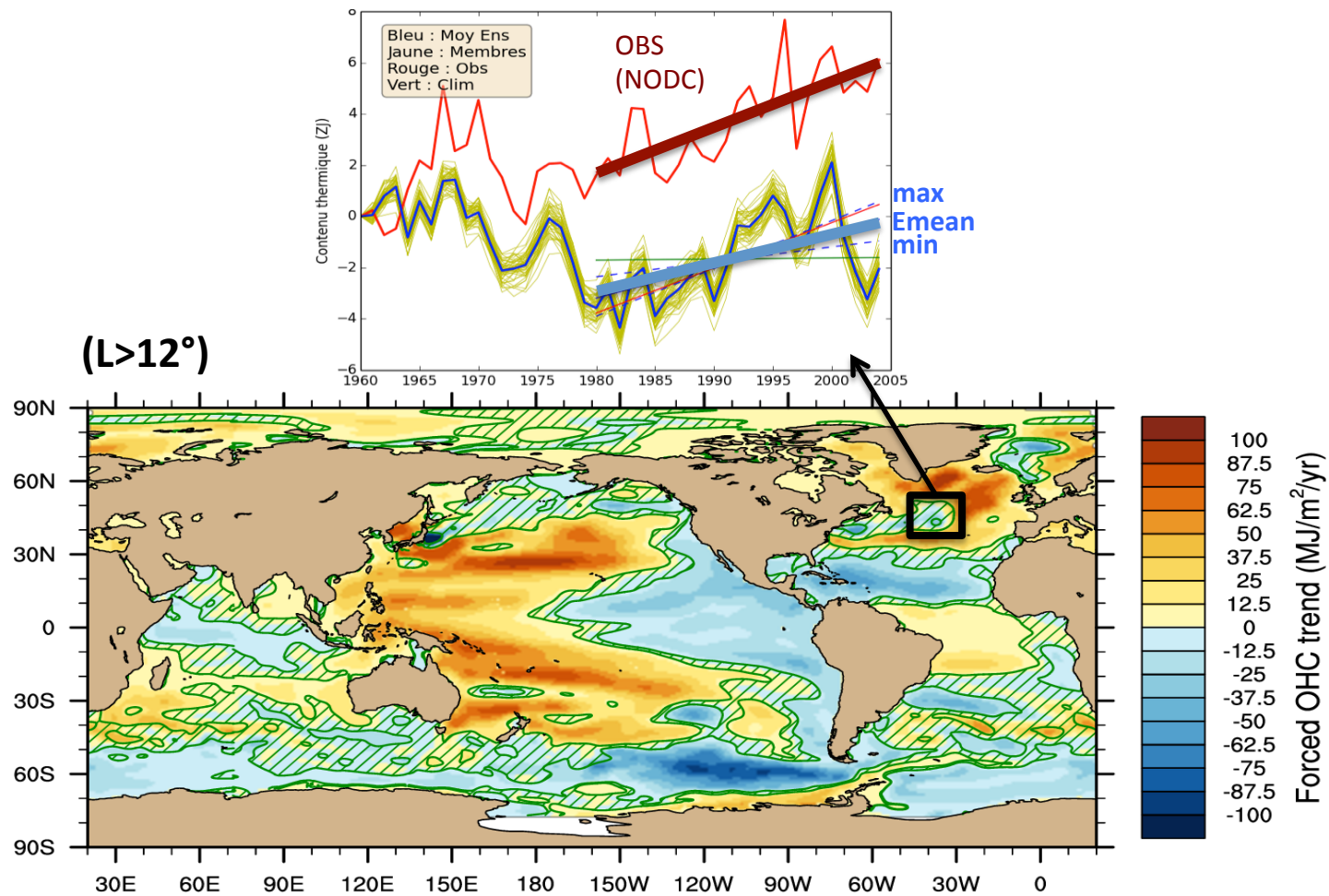
Tstd (Emean) → Forced var.

Tmean (Estd) → Chaotic var.

Green:
Chaotic
exceeds
Forced

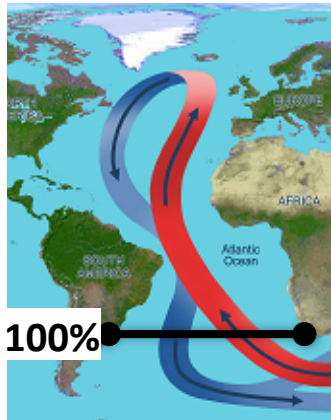


30-year OHC_{0-700m} : Forced vs Chaotic trends (1980-2010)

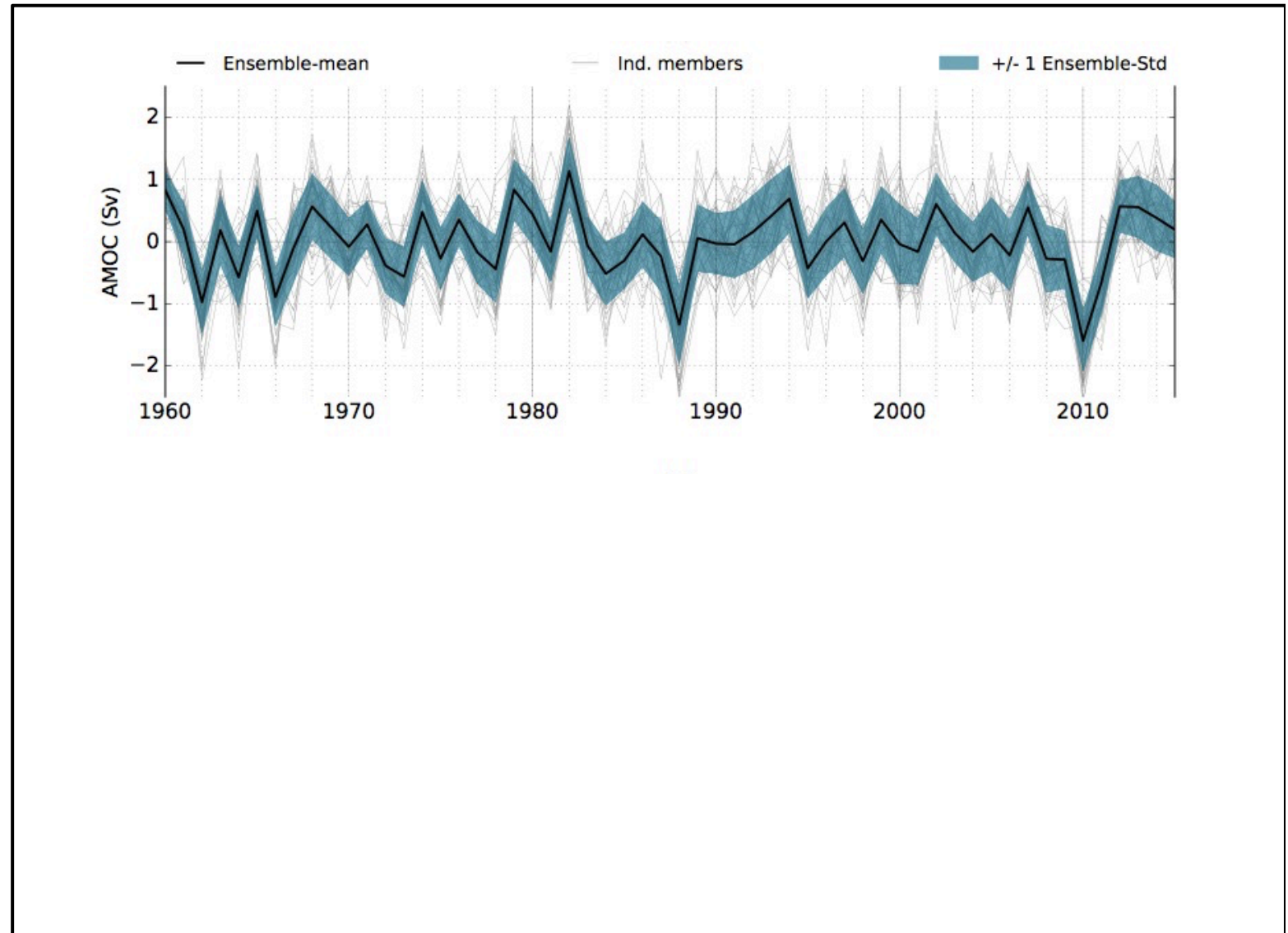


 30-year OHC trends exhibit a large ensemble spread. Trends cannot be unambiguously attributed to the atmospheric forcing

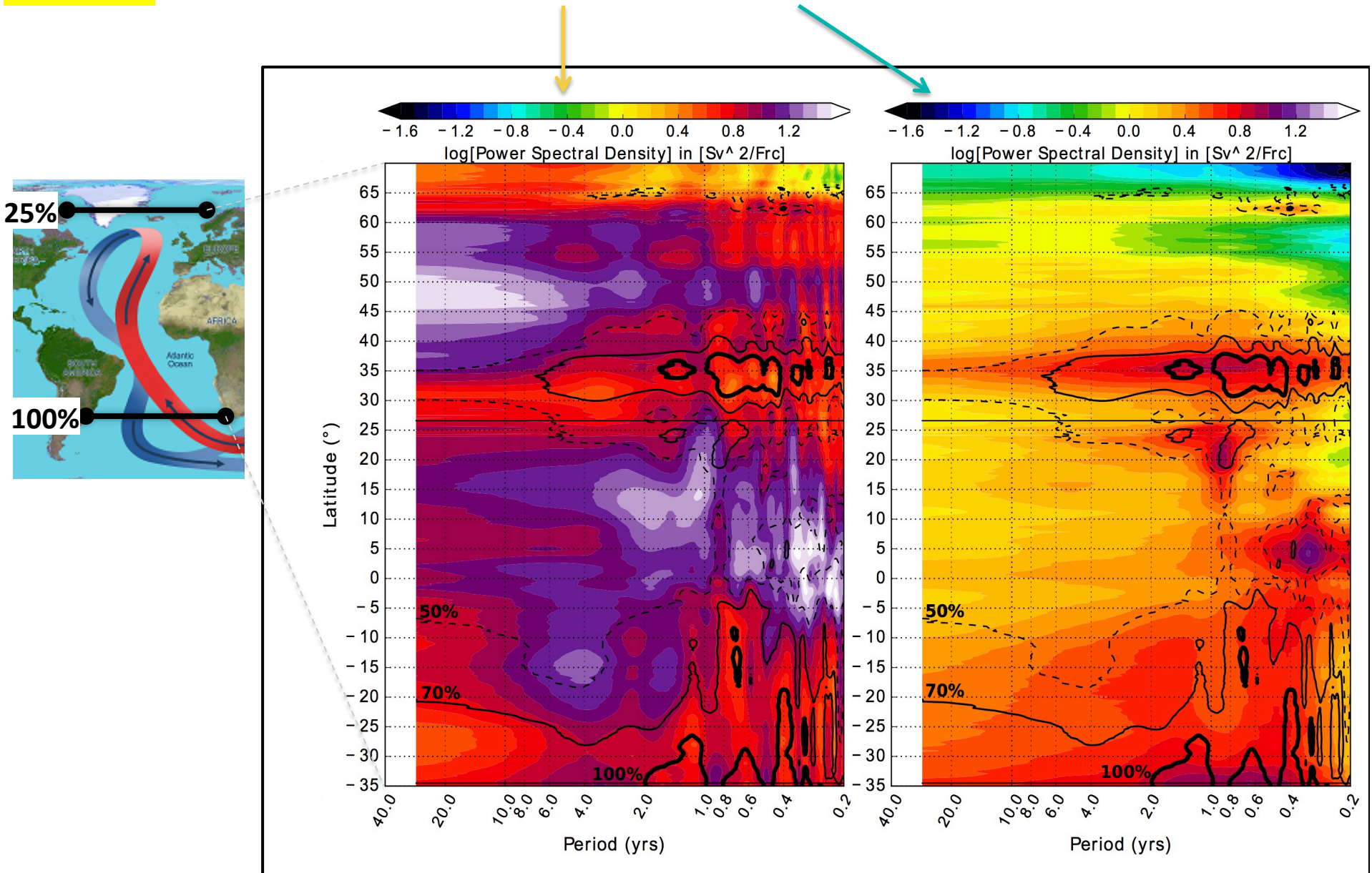
Yearly Atlantic MOC : **Forced** & **Chaotic** STDs (1960-2015)



34.5°S

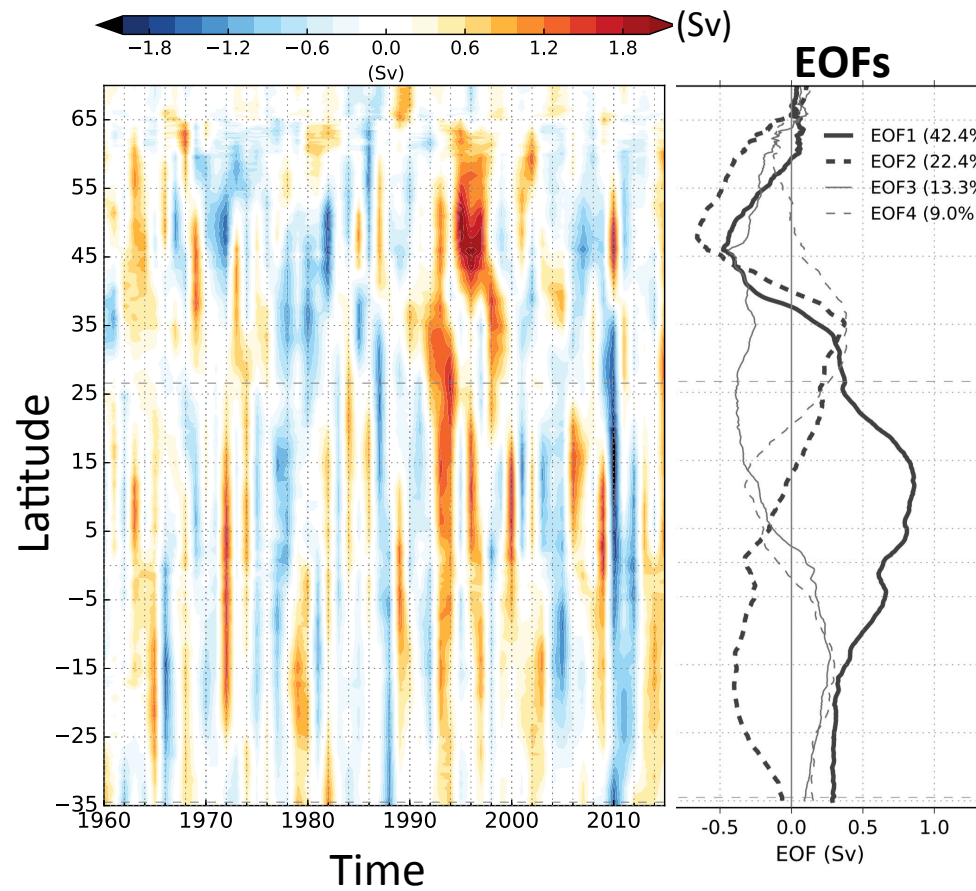


Yearly Atlantic MOC : **Forced** & **Chaotic** spectra (1960-2015)

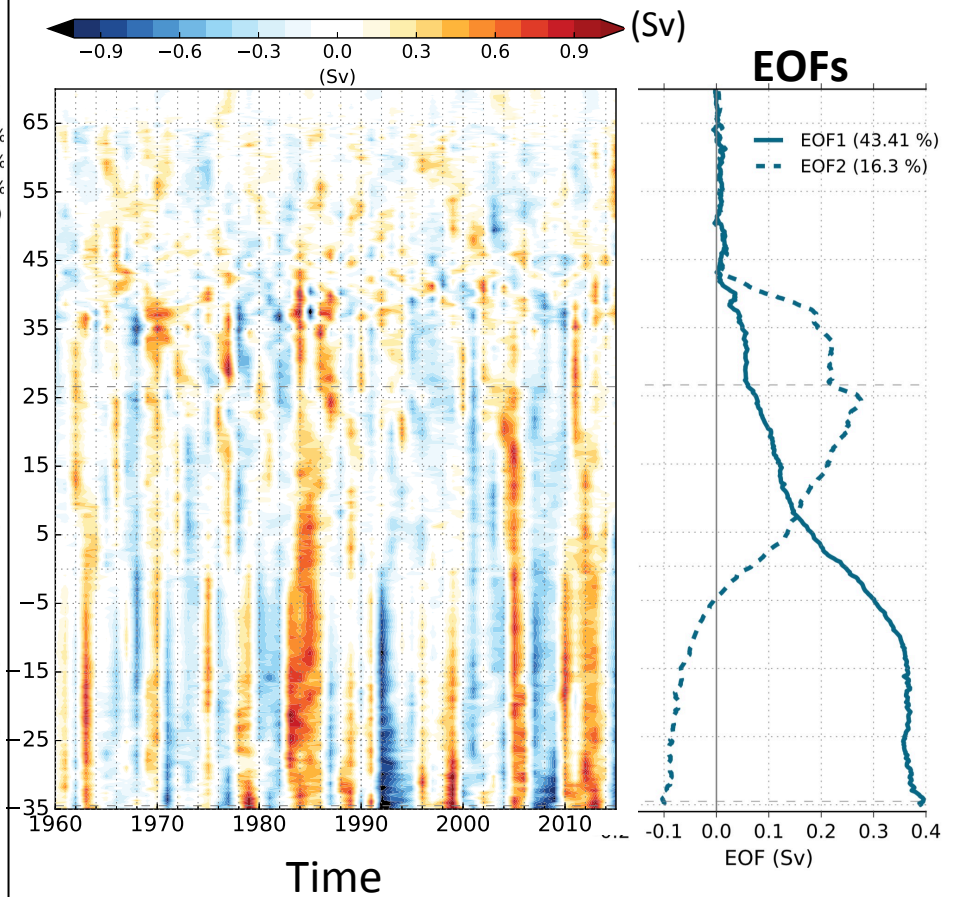


Forced & Intrinsic AMOC interannual variability : latitude-time

Forced AMOC
interannual variability



Chaotic AMOC
interannual variability
(member 1)

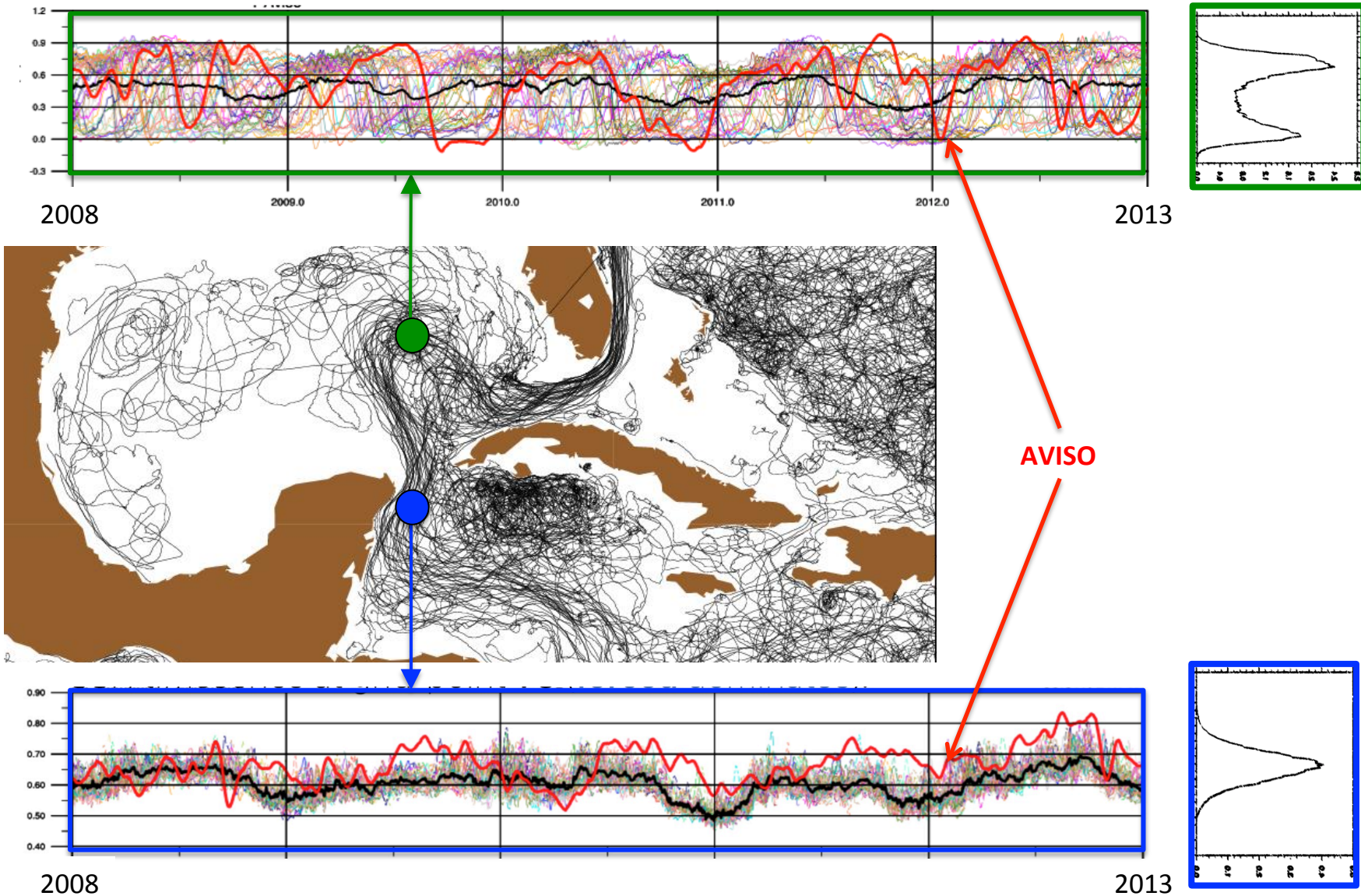


Outline

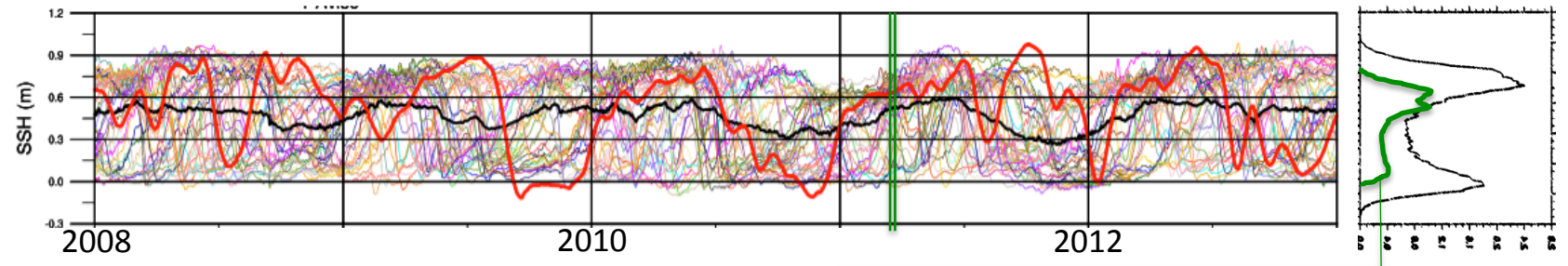
Low-Freq Chaotic Intrinsic Variability in the global ocean

1. LFCIV isolated under seasonal forcing
 - Imprint on observed fields (Sea-level, AMOC)
 - A possible generation mechanism
2. LFCIV modulated by full (reanalyzed) forcing
 - OCCIPUT Ensemble simulations
 - Sea-level, OHC, AMOC
3. New directions and challenges
 - Non-gaussianity, information theory
 - Ocean chaos \leftrightarrow atmosphere
 - Multivariate analyses (MHT – OHC – Qnet)
4. Conclusions and perspectives

Daily SSH: contrasted dynamical regimes



Daily SSH: atmospherically-modulated, non-gaussian Chaotic variab.



Daily entropy :
$$S(x, y, t) = \sum_{i=1}^{50} -p_i(x, y, t) \cdot \log_2(p_i(x, y, t))$$



Disorder/chaos	None	Max
Forcing constraint	Max	None

- Oceanic chaos increases S
- Atmosphere forces low S values
- Hurricanes force S = 0
- Ocean propagates S

Outline

Low-Freq Chaotic Intrinsic Variability in the global ocean

1. LFCIV isolated under seasonal forcing
 - Imprint on observed fields (Sea-level, AMOC)
 - A possible generation mechanism
2. LFCIV modulated by full (reanalyzed) forcing
 - OCCIPUT Ensemble simulations
 - Sea-level, OHC, AMOC
3. New directions and challenges
 - Non-gaussianity, information theory
 - Ocean chaos \leftrightarrow atmosphere
 - Multivariate analyses (MHT – OHC – Qnet)
4. Conclusions and perspectives

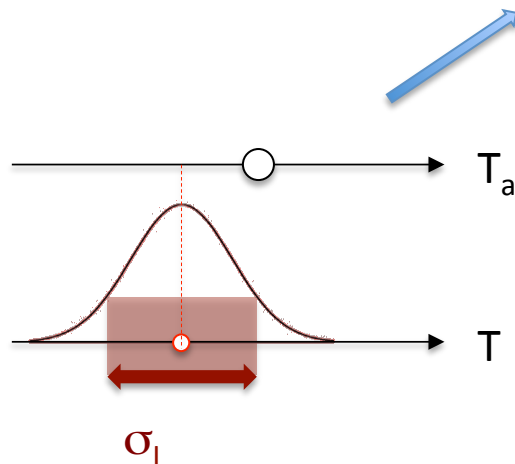
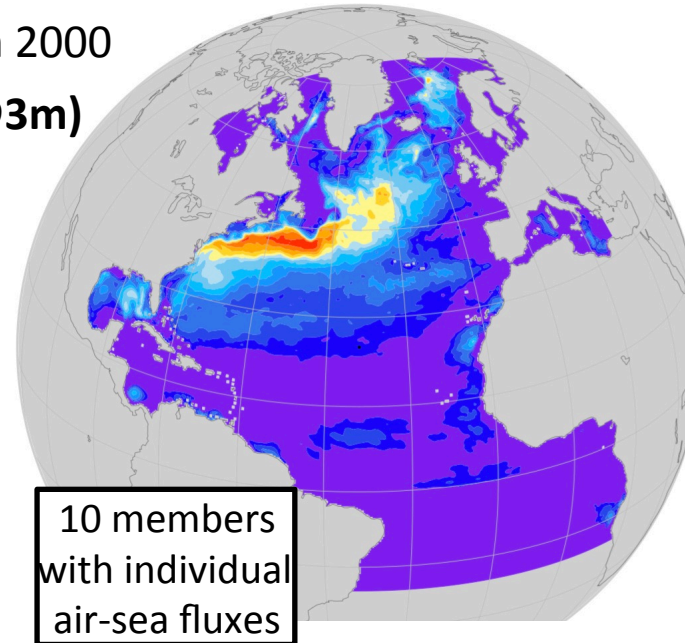
Monthly SST: Turbulent air-sea fluxes and Chaotic variability

10-member NATL025



Jan 17th 2000

$\sigma_c(T@3m)$



Member i : T change due to turbulent air-sea flux

$$Q_{turb}^i = \partial_t T^i = -\lambda(T^i - T_a) \quad T^i \text{ is relaxed toward } T_a$$

$\lambda \sim 1/40$ days
(Barnier, 1998)

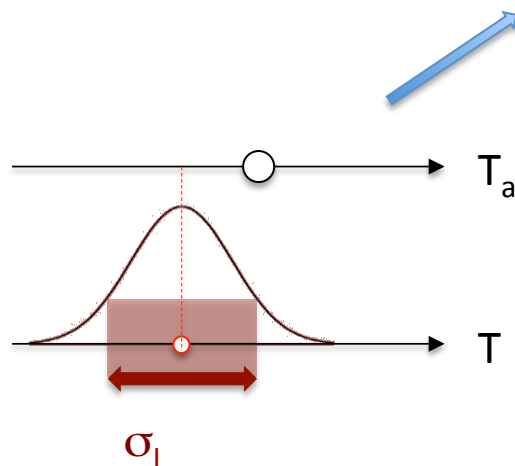
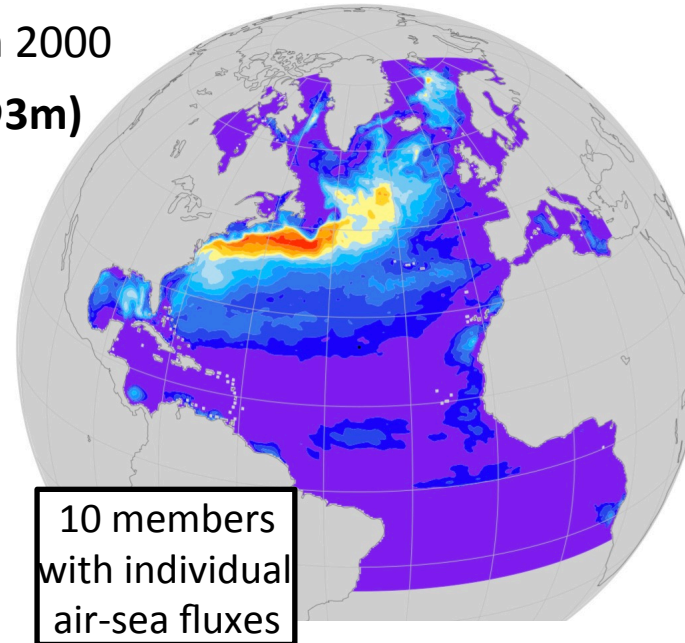
Monthly SST: Turbulent air-sea fluxes and Chaotic variability

10-member NATL025



Jan 17th 2000

$\sigma_c(T@3m)$



Member i : T change due to turbulent air-sea flux

$$Q_{turb}^i = \partial_t T^i = -\lambda(T^i - T_a) \quad T^i \text{ is relaxed toward } T_a$$

$$\text{Forced} \quad \partial_t \langle T \rangle = -\lambda(\langle T \rangle - T_a) \quad \langle T \rangle \text{ is relaxed toward } T_a$$

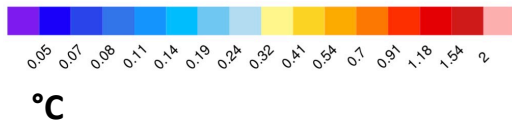
$$\text{Chaotic} \quad \partial_t T^{*i} = -\lambda(T^{*i})$$

$$T^i = \langle T \rangle + T^{*i}$$

$\lambda \sim 1/40$ days
(Barnier, 1998)

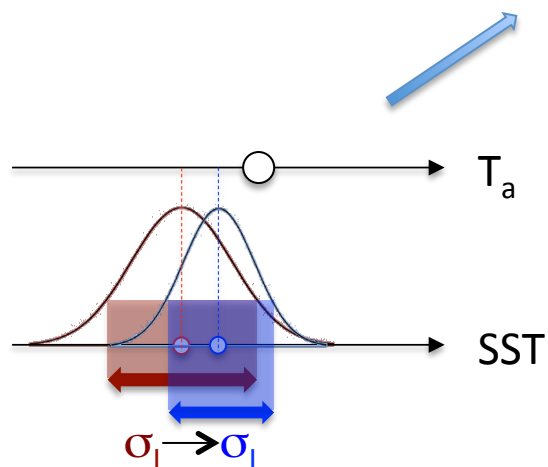
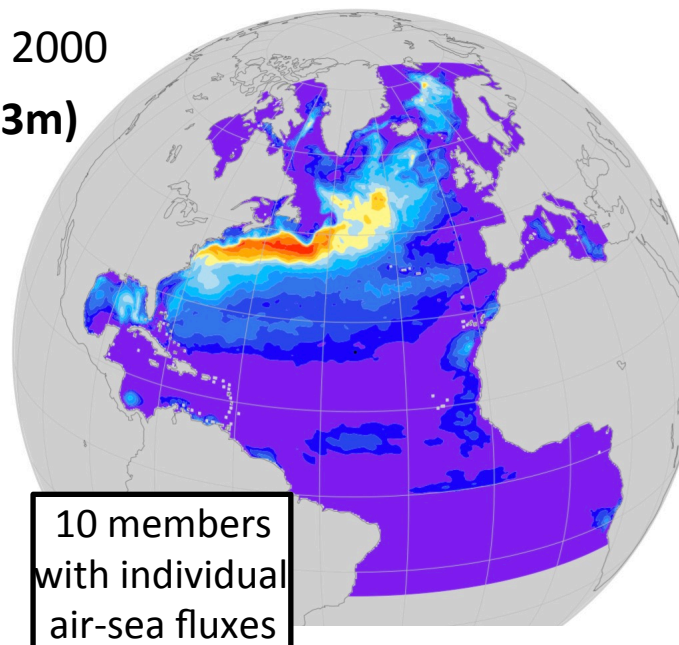
Monthly SST: Turbulent air-sea fluxes and Chaotic variability

10-member NATL025



Jan 17th 2000

$\sigma_c(T@3m)$



Member i : T change due to turbulent air-sea flux

$$Q_{turb}^i = \partial_t T^i = -\lambda(T^i - T_a) \quad T^i \text{ is relaxed toward } T_a$$

$$\text{Forced} \quad \partial_t \langle T \rangle = -\lambda(\langle T \rangle - T_a) \quad \langle T \rangle \text{ is relaxed toward } T_a$$

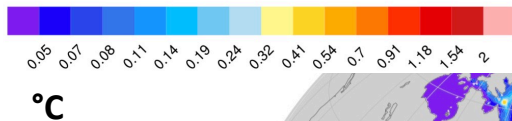
$$\text{Chaotic} \quad \partial_t \sigma_I^2 = -\lambda \cdot \sigma_I^2 \quad \sigma_I \text{ (chaotic) is damped}$$

$$T^i = \langle T \rangle + T^{*i}$$

$\lambda \sim 1/40$ days
(Barnier, 1998)

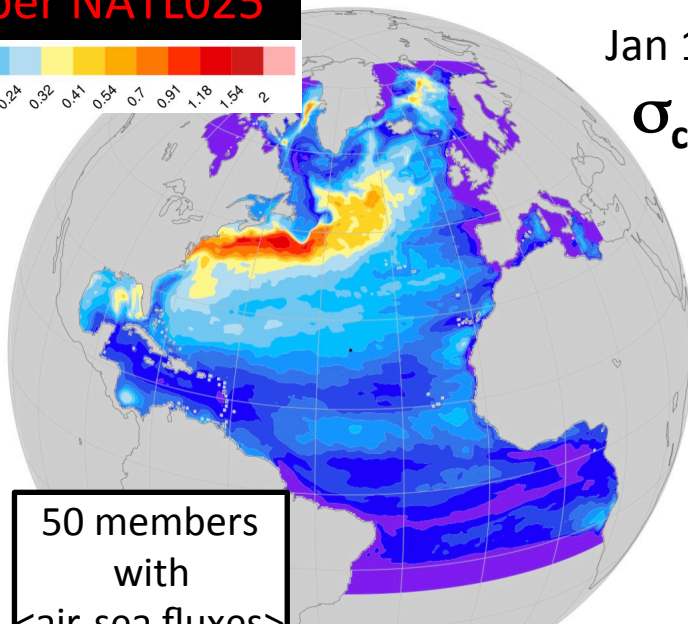
Monthly SST: Turbulent air-sea fluxes and Chaotic variability

10-member NATL025

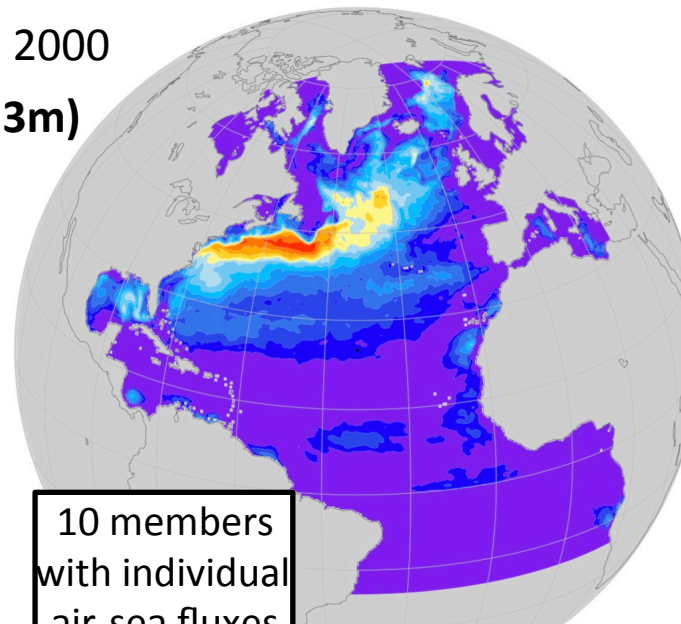


Jan 17th 2000

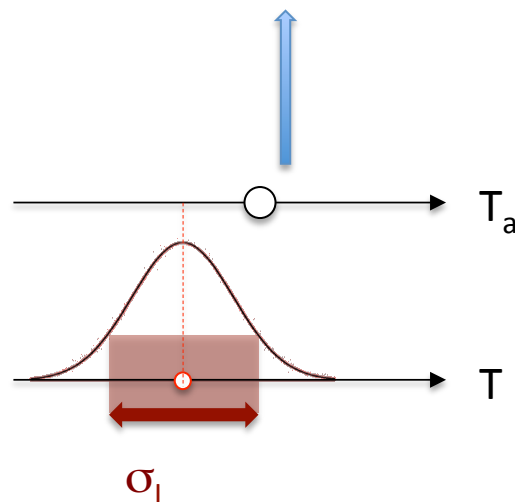
$\sigma_c(T@3m)$



50 members
with
<air-sea fluxes>



10 members
with individual
air-sea fluxes



Member i : T change due to <turbulent air-sea flux>

$$\langle Q_{turb} \rangle = \partial_t T^i = -\lambda(\langle T \rangle - T_a) \quad T^i \text{ is relaxed toward } T_a$$

Forced $\partial_t \langle T \rangle = -\lambda(\langle T \rangle - T_a)$ $\langle T \rangle$ is relaxed toward T_a

Chaotic $\partial_t T^{*i} = 0$ σ_l (chaotic) is untouched

$$T^i = \langle T \rangle + T^{*i}$$

$\lambda \sim 1/40$ days
(Barnier, 1998)

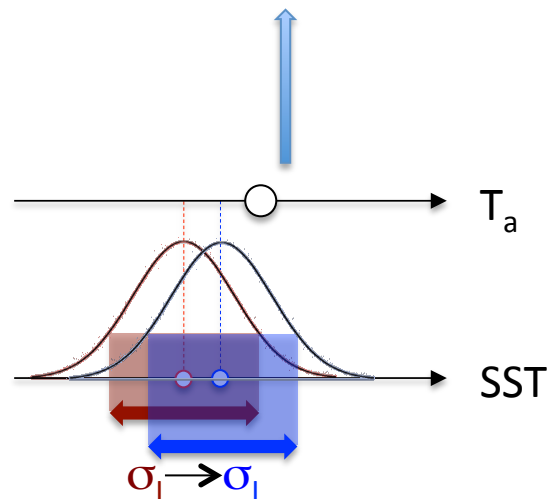
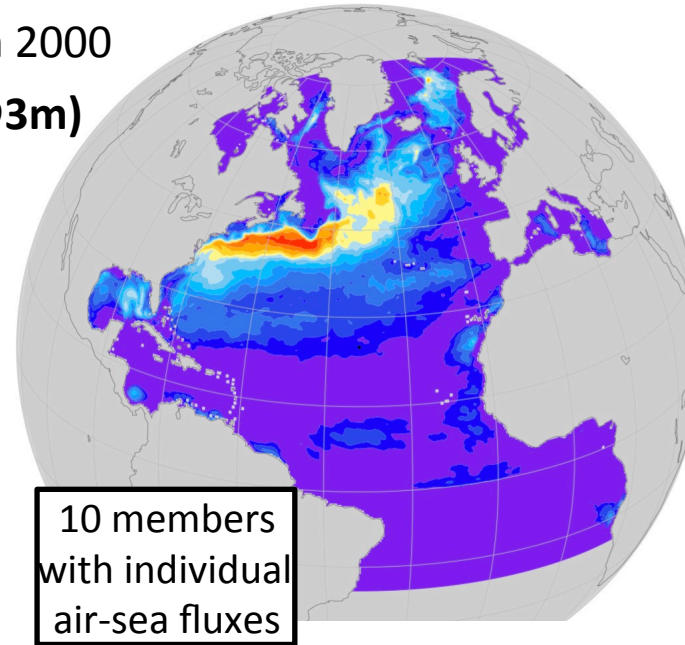
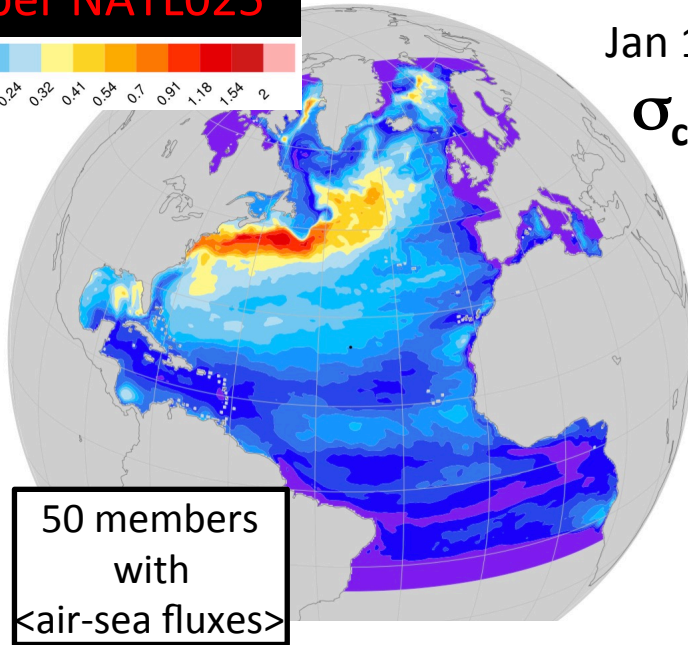
Monthly SST: Turbulent air-sea fluxes and Chaotic variability

10-member NATL025



Jan 17th 2000

$\sigma_c(T@3m)$



Member i : T change due to <turbulent air-sea flux>

$$\langle Q_{turb} \rangle = \partial_t T^i = -\lambda(\langle T \rangle - T_a) \quad T^i \text{ is relaxed toward } T_a$$

Forced $\partial_t \langle T \rangle = -\lambda(\langle T \rangle - T_a)$ $\langle T \rangle$ is relaxed toward T_a

Chaotic $\partial_t \sigma_I^2 = 0$ σ_I (chaotic) is untouched

$$T^i = \langle T \rangle + T^{*i}$$

$\lambda \sim 1/40$ days
(Barnier, 1998)

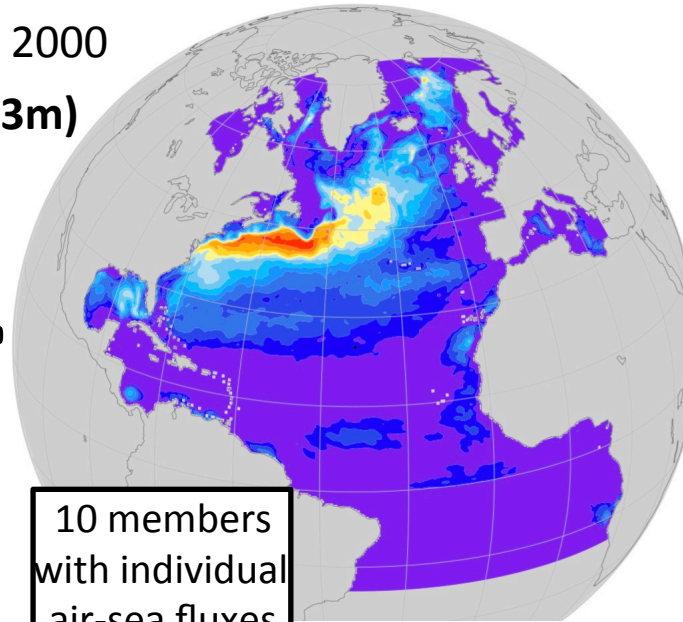
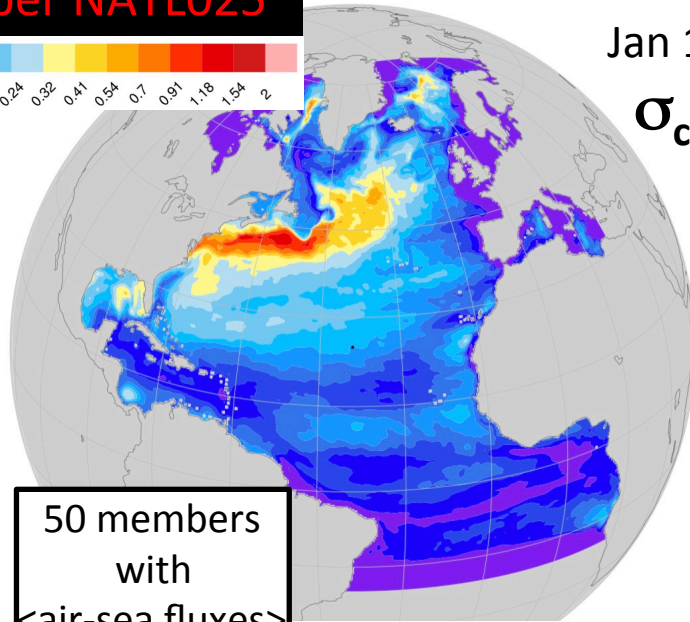
Monthly T : Turbulent air-sea fluxes and Chaotic variability

10-member NATL025

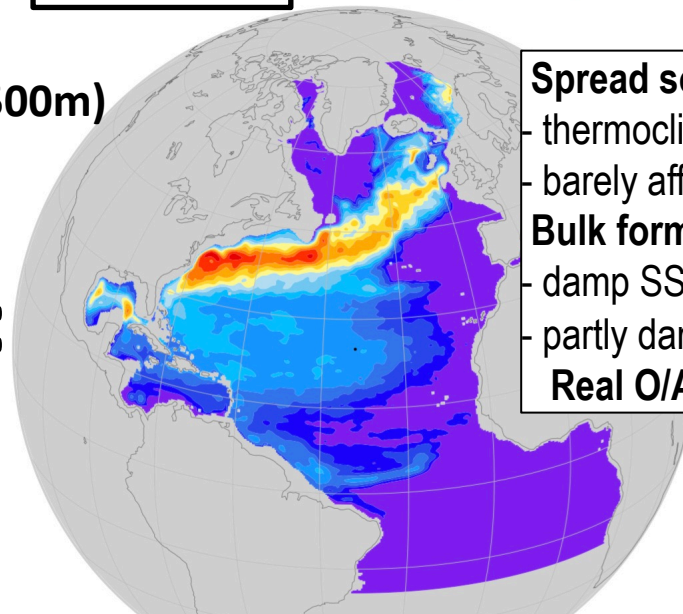
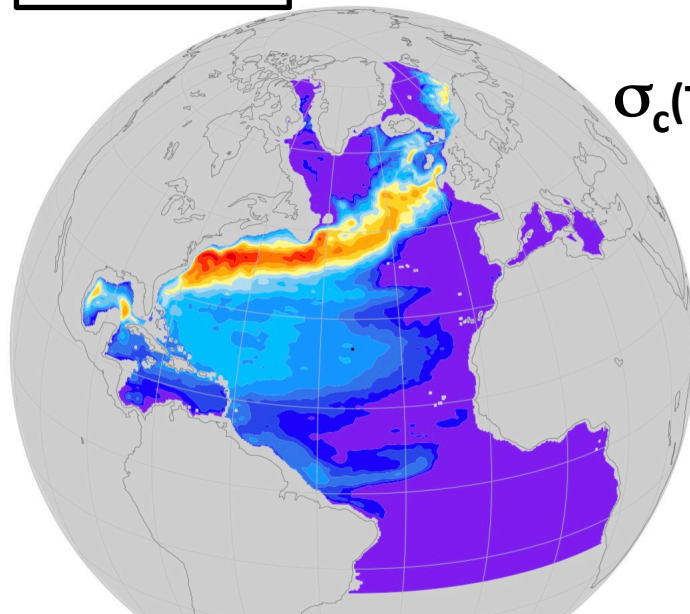


Jan 17th 2000

$\sigma_c(T@3m)$



$\sigma_c(T@500m)$



Spread source
- thermocline depth
- barely affected by bulks
Bulk formulae
- damp SST spread
- partly damp OHC spread
Real O/A inbetween?

Outline

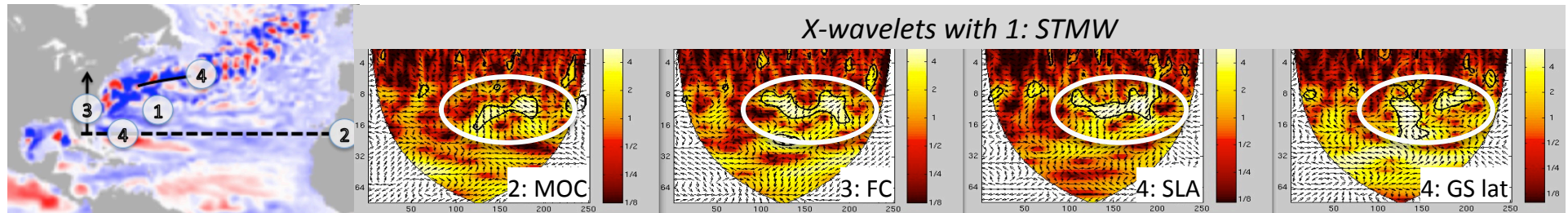
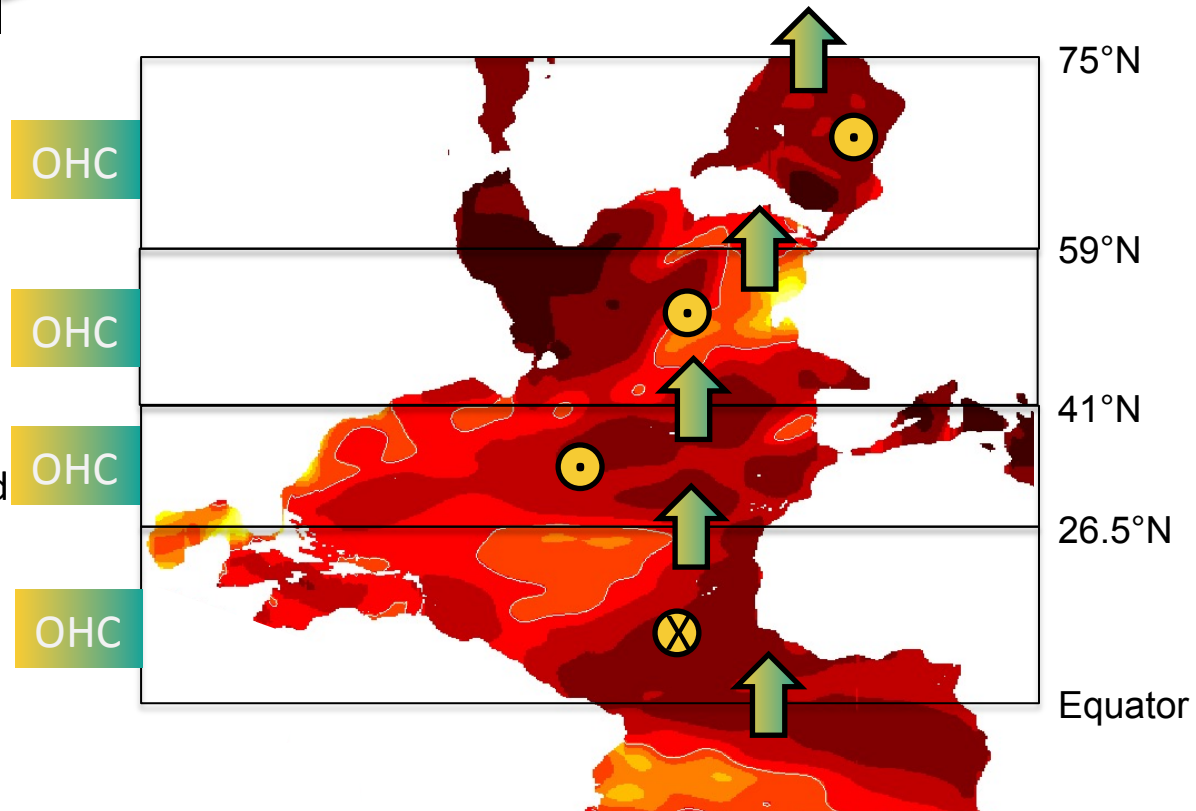
Low-Freq Chaotic Intrinsic Variability in the global ocean

1. LFCIV isolated under seasonal forcing
 - Imprint on observed fields (Sea-level, AMOC)
 - A possible generation mechanism
2. LFCIV modulated by full (reanalyzed) forcing
 - OCCIPUT Ensemble simulations
 - Sea-level, OHC, AMOC
3. New directions and challenges
 - Non-gaussianity, information theory
 - Ocean chaos \leftrightarrow atmosphere
 - Multivariate analyses (MHT – OHC – Qnet)
4. Conclusions and perspectives

Forced & Intrinsic multivariate/multiscale variability

Forced
Chaotic
 $\rightarrow \partial_t OHC = Q_{net} + (MHT_{south} - MHT_{north})$

chaos controls 25% of the OHC LF/LS std



Outline

Low-Freq Chaotic Intrinsic Variability in the global ocean

1. LFCIV isolated under seasonal forcing
 - Imprint on observed fields (Sea-level, AMOC)
 - A possible generation mechanism
2. LFCIV modulated by full (reanalyzed) forcing
 - OCCIPUT Ensemble simulations
 - Sea-level, OHC, AMOC
3. New directions and challenges
 - Non-gaussianity, information theory
 - Ocean chaos \leftrightarrow atmosphere
 - Multivariate analyses (MHT – OHC – Qnet)
4. Conclusions and perspectives

Conclusions & Perspectives

◆ Low-frequency ($T > 1$ year) ocean variability

- Laminar models (2°) : ~100% Forced → *Deterministic hindcasts OK*
- Eddying models ($1/4^\circ, 1/12^\circ$) : Atmospherically-modulated **chaos** (OHC, SST, MOC, SSH, etc)
Chaotic var. : strong, up to multidecadal/basin scales (MOC, OHC, SST...)
Poorly-known & complex → *Probabilistic hindcasts required*

◆ Open questions & perspectives

- (multiple) dynamical processes, energetics, etc ? → *GFD studies, idealized simulations*
- Oceanic chaos → D/A of climate variability / change? → *Ensemble synthetic observations*
- Oceanic chaos → air-sea fluxes → atmosphere/climate ? → *Investigations starting*
- Collaborative investigations → *OCCIPUT data subsets*

SLA : Penduff et al (J. Clim 2011)
Scales : Sérazin et al (J. Clim 2015)
MOC, MHT : Grégorio et al (JPO 2015)
OCCIPUT : Penduff et al (Clivar Exch. 2014)
Ensemble NEMO : Bessières et al (GMD 2017)

SLA (D & A) : Sérazin et al (GRL 2016)
OHC : Sérazin et al (GRL 2017)
MOC : Leroux et al (J. Clim in rev)
Temporal inv. casc. : Sérazin et al (JPO subm.)